

**ICDEA 2016**

**The 22nd International Conference on  
Difference Equations and Applications**

**Osaka, Japan**

**July 24 to 29, 2016**

**Abstracts Book**

# Program of ICDEA2016

<b>Sunday, July 24</b>	
<b>Time</b>	<b>I-site Namba 2F</b>
16:00-17:00	Registration

<b>Monday, July 25</b>		
<b>Time</b>	<b>I-site Namba 2F</b>	
08:45-09:30	Registration	
	Conference Room 2 + Room 3	
	<b>Chair</b>	<b>Speaker and Title</b>
09:30-09:40	Yamaoka	Opening
09:40-10:40	Cushing	Saber Elaydi (USA), Global Dynamics of Difference Equations: Applications to Population Dynamics
10:40-11:00	Coffee Break	
11:00-12:00	Schreiber	Ryusuke Kon (Japan), Bifurcations in nonlinear Leslie matrix models
12:00-14:00	Lunch	
Session 1	Conference Room 3	
14:00-14:25	Kon	Youssef Raffoul (USA), Boundedness of Solutions in Almost Linear Volterra Difference Equations Using Fixed Point Theory and Lyapunov Functionals
14:25-14:50	Kon	Yukihiko Nakata (Japan), Stability of a logistic equation with multiple delays
14:50-15:15	Raffoul	Kaori Saito (Japan), On the Stability of an SIR epidemic discrete model with a delay
15:15-15:40	Raffoul	Inese Bula (Latvia), About neuron model with period two and three internal decay rate
15:40-16:00	Coffee Break	

## Monday, July 25

Session 1		
Conference Room 3		
Time	Chair	Speaker and Title
16:00-16:25	Nakata	Shinji Nakaoka (Japan), Exploration of combinatorial emergence in coupled boolean network systems
16:25-16:50	Nakata	Mansoor Saburov (Malaysia), Applications of non-autonomous discrete dynamical systems into nonlinear consensus problems
16:50-17:15	Nakaoka	Kuo-Chih Hung (Taiwan), Allee effect and its applications
17:15-17:40	Nakaoka	Wirot Tikjha (Thailand), Prime period 4 behavior of certain piecewise linear system of difference equations where initial condition are some points in positive x-axis
18:30-20:30	Welcome Party	

Session 2		
Conference Room 1		
Time	Chair	Speaker and Title
14:00-14:25	Nishimura	Aiko Tanaka (Japan), An evolutionary game model of families' voluntary provision of public goods
14:25-14:50	Nishimura	Takashi Honda (Japan), Operator theoretic phenomena of the Markov operators which are induced by stochastic difference equations
14:50-15:15	Nishimura	Ryoji Hiraguchi (Japan), On a solution path to the optimal growth model with multiplicative habits
15:15-15:40	Nishimura	Takuma Kunieda (Japan), Asset Bubbles, Financial Crisis, and Unemployment
15:40-16:00	Coffee Break	
16:00-16:25	D'Aniello	Hikmet Kemaloglu (Turkey), Uniqueness of Potential Function in Sturm-Liouville Difference Equation
16:25-16:50	D'Aniello	Yan-Hsiou Cheng (Taiwan), Eigenvalue estimates for the Sturm- Liouville equation
16:50-17:15	Kemaloglu	Petr Zemánek (Czech Republic), Self-adjoint extensions of minimal linear relation associated with discrete symplectic system
17:15-17:40	Kemaloglu	Nobuyuki Higashimori (Japan), Convergence of finite difference schemes applied to the Cauchy problems of quasi-linear partial differential equations of the normal form
18:30-20:30	Welcome Party	

# Applications of non-autonomous discrete dynamical systems into nonlinear consensus problems

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Historically, an idea of reaching consensus through repeated averaging was introduced by DeGroot (see [1, 3]) for a structured *time-invariant* and synchronous environment. Since that time, the consensus which is the most ubiquitous phenomenon of multi-agent systems becomes popular in various scientific communities, such as biology, physics, control engineering and social science. Roughly speaking, a trajectory of a row-stochastic matrix presents DeGroot's model of the structured *time-invariant* synchronous environment. In [2], Chatterjee and Seneta considered a generalization of DeGroot's model for the structured *time-varying* synchronous environment. A trajectory of a sequence of row-stochastic matrices (a non-homogeneous Markov chain) presents the Chatterjee-Seneta model of the structured *time-varying* synchronous environment.

In this paper, we shall consider a *nonlinear model of the structured time-varying synchronous environment* which generalizes both DeGroot's and the Chatterjee-Seneta models. Namely, by means of multidimensional stochastic hypermatrices, we present an opinion sharing dynamics of the multi-agent system as a trajectory of non-autonomous polynomial stochastic operators (nonlinear Markov operators). We show that the multi-agent system eventually reaches to a consensus under suitable conditions.

## References

- [1] R. L. Berger, *A necessary and sufficient condition for reaching a consensus using DeGroot's method*, J. Amer. Stat. Assoc. 76 (1981) 415–418.
- [2] S. Chatterjee and E. Seneta, *Towards consensus: some convergence theorems on repeated averaging*, J. Appl. Prob. 14 (1977) 89–97.
- [3] M. H. DeGroot, *Reaching a consensus*, J. Amer. Stat. Assoc. 69 (1974) 118–121.